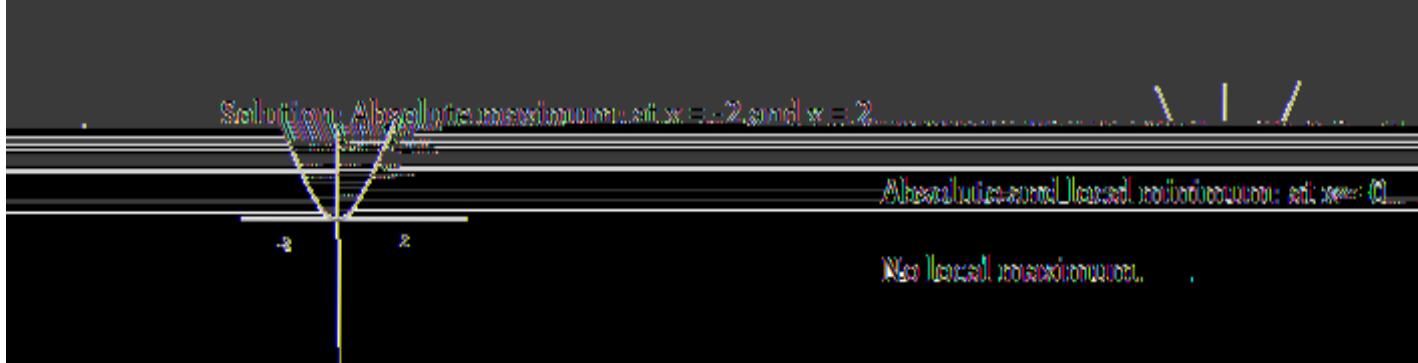


# MAXIMA AND MINIMA

**Absolute Maximum:** Let  $f$  be defined on an interval  $I$ , and



**Example:** Interpret the absolute maximum and minimum values based on the graph.



and there exists a point  $c \in I$  (domain of  $f$ ), then  $c$

**Critical Points:** Let  $f$  be defined on an interval  $I$ , if

then  $c$  is called a critical point of  $f$ . Critical points are also called stationary points.

Ex. Find the critical points of  $f(x) = x^3 - 3x^2 + 2$ .

# MAXIMA AND MINIMA

$$\text{Given: } f(x) = 2x^5 - 5x^3 \quad \text{on the interval } [-1, 2]$$

in the interval  $[-1, 2]$

b.)  $g(x) = x^{2/3}(2-x)$

Solution:

polynomial, thus it's derivative exists everywhere. Now let's find the critical. a.) We know that  $f$  is a polynomial, thus its derivative exists everywhere. Now let's find the critical.

critical points:  $x=0$ , and  $x=\frac{3}{2}$ , and both of these points are... Solving this equation gives us two criti.

critical points:  $x=0$ , and  $x=\frac{3}{2}$ . Now to find the critical points up; differentiate the function.

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critical points:  $x=0$ , and  $x=\frac{3}{2}$ . Now we see that  $x=0$  is a critical point because

:  $x=0$  and  $x=\frac{4}{5}$ . Now we will check the values of the function at the critical points, because we find the maximum and minimum values of the function.

Thus we see that the function attains the largest value at  $x=-1$  and the smallest at  $x=0$  and  $x=2$ .

The absolute minimum of  $g$  on  $[-1, 2]$  is 0.

$g(-1) = 3$ ,  $g(0) = 0$ ,  $g(4/5) = 1.03$  and  $g(2) = 0$ .

Therefore, absolute maximum of  $g$  on  $[-1, 2]$  is 3 and

